

GCSE MARKING SCHEME

SUMMER 2019

GCSE
MATHEMATICS – NUMERACY
UNIT 2 - INTERMEDIATE TIER
3310U40-1

INTRODUCTION

This marking scheme was used by WJEC for the 2019 examination. It was finalised after detailed discussion at examiners' conferences by all the examiners involved in the assessment. The conference was held shortly after the paper was taken so that reference could be made to the full range of candidates' responses, with photocopied scripts forming the basis of discussion. The aim of the conference was to ensure that the marking scheme was interpreted and applied in the same way by all examiners.

It is hoped that this information will be of assistance to centres but it is recognised at the same time that, without the benefit of participation in the examiners' conference, teachers may have different views on certain matters of detail or interpretation.

WJEC regrets that it cannot enter into any discussion or correspondence about this marking scheme.

WJEC GCSE MATHEMATICS - NUMERACY (3310U40-1)

SUMMER 2019 MARK SCHEME

GCSE Mathematics - Numeracy Unit 2: Intermediate Tier	Mark	Comments
1(a)(i) 80 ± 2 or 20 360 90	M1	Allow use of '÷' for M1
<u>2</u> 9	A1	FT only when simplifying possible, 78/360 = 13/60 81/360 = 9/40 82/360 = 41/180
1(a)(ii) A correct numerator or denominator in any of the following proper fractions:	M1	Must be in a proper fraction
3.5 or 14 or 7 14.5 58 29		Allow for sight of 3.5 ÷ 14.5 or 14 ÷ 58 or 7 ÷ 29
<u>7</u> 29	A1	
1(b) Sight of <u>2</u> (× 100) or <u>8</u> (× 100) 14.5 58	M1	FT 'their 14.5' or 'their 58' from (a)(ii) provided ≠ 90 If restarting, allow an error in a convincing sum to 'their total' for M1, but A0
13.79(%) or 13.8(%) or 14(%)	A1	Do not accept 13(%) or 13.7(%) (but unsupported this does imply M1)
1(c) (Ffordd Owain) $140(^{\circ}) \pm 2(^{\circ})$ $140 \pm 2 \times 90$ or $(140 \pm 2) \times 90 \div 360$ 360 or $(140 \pm 2) \div 360/90$	B1 M1	May be seen by Saturday on the pie chart
35 (pairs)	A1	May be seen by Saturday on the pie chart Answer must be a whole number.
(Arthur Avenue 4 × 4 =) 16 (pairs of sunglasses)	B1	Accept 16 shown on the pictogram unambiguously for Saturday
(Difference) 19 (pairs of sunglasses)	B1	FT 'their Ffordd Owain total' – 'their Arthur Avenue total' for Saturday, provided 'their Ffordd Owain total' ≠ 90 and ≠ 140 ± 2, and 'their Arthur Avenue total' ≠ 4

2(a)		Ignore incorrect units or lack of units for M, A and E
Method to compare, e.g. • (Per kg price in SuperM) 1000 × 27 ÷ 450 • (1g cost of each, SuperM and FairMart) 27 ÷ 450 and 57 ÷ 1000 • (g per penny for SuperM and FairMart) 450 ÷ 27 and 1000 ÷ 57 • (450g at Fairmart) 57 × 450 ÷ 1000 • (SuperM) 11 × 450(g) with 11× 27(p) AND (Fairmart) 5 × 1000(g) with 5 × 57(p)	M1	marks Needs to show comparing like quantity with like, unless considering larger quantities where working shows a greater quantity for less money at Fairmart (e.g. 4950g with 5000g)
Accurate comparison calculation, e.g. (Per kg price in SuperM) 60(p) (1g cost of each, SuperM and FairMart) 0.06(p) and 0.057(p) (g per penny for SuperM and FairMart) 16.6(66 g per penny and 17.5(4 g per penny) (450g at Fairmart) 25.65 (p) (< 27p) (SuperM) 4950(g) for (£)2.97 AND (Fairmart) 5000(g) for (£)2.85	A1	In cost per kg in SuperM, allow truncation of (1000 ÷ 450 =) 2.222 to 1 or more decimal places to give 59.4, 59.94, 59.994, etc when × 27(p) Accept comparison given in pence 1 g
Conclusion, e.g. '(Buying carrots from) FairMart (is better value for money.)'	E1	FT for 'their costs' provided M1 previously awarded
Organisation and communication	OC1	For OC1, candidates will be expected to: • present their response in a structured way • explain to the reader what they are doing at each step of their response • lay out their explanations and working in a way that is clear and logical • write a conclusion that draws together their results and explains what their answer means
Writing	W1	For W1, candidates will be expected to: • show all their working • make few, if any, errors in spelling, punctuation and grammar • use correct mathematical form in their working • use appropriate terminology, units, etc.
2(b) (Carrots) 2812.5 (g) (Stock) 5 (litres) (Cream) 25 (tablespoons)	B2	Mark recipe card as their final answer if complete Accept 2812(g) or 2813(g) for carrots Allow 2.812(5) k(g) or 2.813 k(g) ('k' must be inserted) B1 for any 2 of these 3 answers correct
(Onions) 12 or 13	B1	Must be a whole number of onions If no marks, award SC1 for answers leading to quantities of carrots, stock and cream in the ratio 450: 0.8: 4, e.g. 5625, 10, 50, or 3150, 5.6, 28, or 11250, 20, 100 provided all quantities are increased

3(a)(i) 18:30, Saturday	B1	
3(a)(ii) 16:00, Saturday	B1	
3(b) 320 ÷ 0.61 or 524(.59) 525 (AUD)	M1 A1	
4(a) 3.25 + 4× 2.4(0) (=) (£)12.85	M1 A1	If no marks, award SC1 for an answer of any of the following: Answer
4(b) (Minimum time) 61 minutes	В3	B2 for an answer of 1 hour 1 minute OR B1 for sight of any one of the following • (8.05–3.25)÷2.4(0) • 3.25 + 2.4(0) + 2.4(0) (= 8.05) • 4.8(0)÷2.4(0) (= 2 hours) • 2 hours OR an answer of a number of minutes >61 but ≤120
5(a)(i) Reason, e.g. 'find out if too far to go swimming', 'find out if there is a pool nearby', 'interesting to explore between distance people live from the pool and how often they use the pool' 'to find out how far people would travel to get to the sports centre', 'show relationship between how frequently they go swimming and distance travelled', 'see how far people travelled', 'to analyse the distance people travelled', 'to find out if people who live close by go more often', 'distance can affect participation'	E1	Allow, e.g. 'to see whether people close by use the gym more', 'shows how far people are willing travel', 'people who live close by go more often', 'distance affects participation' Do not accept, e.g. 'not a biased question', 'anyone can answer it', 'it would give a numerical answer', 'to see how people go to the sports centre', 'data can be grouped', 'data can be analysed'
5(a)(ii) Difficult to analyse because, e.g. 'no categories', 'vague (question)', 'it is not specific', 'need time frame', 'it could be weeks, months, years' 'don't know what often means', 'no time period given', 'it is an open question', 'may not be about swimming in this sports centre'	E1	Do not accept, e.g. 'they may not remember', 'they don't know', 'they might not go swimming'

5(a)(iii) Appropriate question and at least 3 suitable categories with no gaps or overlaps, e.g. 'under 20 minutes, 20 minutes to one hour, more than one hour', '1 hour or less, more than 1 hour but less than 2 hours, 2 hours or more'	B2	Ignore gaps in continuous data provided not greater than 1 minute Allow 2 suitable groups with the third group as 'more' or similar Accept if options do not start at zero, provided the first option starts below 31 minutes Provided an appropriate question is given: Working in minutes allow: • B2 for 0 – 30, 31 – 40, 41 – 50 • B1 for 0 – 30, 30 – 50, 50 – 70 Working in hours allow B1 for any of the following • 0 – 1, 1 – 2, 2 – 3 • 0 – 1, 2 – 3, 4 – 5 Award B1, if the B2 criteria would be met apart from having any one of the following errors: • First option starts between 31 minutes and 1 hour as lower bound, • There is a missing or inappropriate question • Poor or incorrect use of inequalities is seen
5(b)(i) 4 (°C)	B1	(28 – 24 = 4) Do not accept from incorrect working, e.g. 29 – 25
5(b)(ii) 36 (minutes)	B1	Accept answers in the inclusive range 35 minutes to 37 minutes
6(a)(i) 8	B1	
6(a)(ii) 180	B1	
6(a)(iii) Sight of total 403	B1	FT 'their 180' + 223
(100 ×) <u>15</u> or (100 ×) 15 ÷ 403	M1	FT correctly evaluated 'their 180' + 223
3.7 (%)	A2	Mark final answer A1 for 3.72(%) or from correct working 4(%) If no marks, award SC1 for 100 ×15 ÷'their total' correctly evaluated or SC2 for this answer rounded correctly to 1 decimal place
		(Note: SC1 for 100 × 15 ÷ 388 = 3.8(6%) or SC2 if rounded to 3.9(%))

6(b) 72 000	B1	
6(c) Sight of 9.95 (m) or 99.95(m) or 995 (cm) or 9995 (cm)	B1	If units are given they must be correct
(Least length) 9.95 + 99.95 + 9.95 or equivalent in cm	M1	FT 'their least measurements' x and y, provided $9.9 \text{ (m)} \le x < 10 \text{ (m)}$ and $99.9 \text{ (m)} \le y < 100 \text{ (m)}$ as appropriate
119.85 (m)	A1	CAO Award all 3 marks for a correct response
		If no marks, award SC1 for an answer of 118.5(m) or 119.985(m) or (9.95 + 9.95 + 99.5 =) 119.4(m)
6(c) Alternative method: 100 + 10 + 10 – 3 × 0.05 or equivalent in cm 119.85 (m)	M2 A1	M1 for sight of - 5 cm or -0.05 (m) used CAO If no marks, award SC1 for an answer of 119.7.(m)
7(a)(i) (Volume) $\pi \times 3.6^2 \times 9.3$ Answer in the range 378.4 (cm³) to 378.7 (cm³) 378 (cm³) or 379 (cm³)	M1 A1	Mark final answer
7(a)(ii) 189 (g) or an answer in the range 189.2 (g) to 189.5 (g)	B1	Allow rounding or truncation to whole number or a number of decimal places FT, for a similar range, 'their 379' accurately divided by 2
7(b) (Height is) 9.3 × 4.2 ÷ 3.6 or 1.16666 × 9.3 or 9.3 ÷ (3.6 ÷ 4.2) or equivalent	M1	Allow M1 for 1.16 × 9.3 or 1.17 × 9.3 or 9.3 ÷ 0.85(7)
10.85 (cm)	A1	Allow answers in the inclusive range 10.78 (cm) to 10.95 (cm)

7(c) Comparison of salt and sugar, e.g.	B1	Or equivalent
• (Salt) 6 AND (Sugar) 90	D1	Of equivalent
1.85 11.7		Ignore any units given
• (Salt)(100×) <u>1.85</u> AND (Sugar)(100×) <u>11.7</u>		
6 90		
• (Recommend) 1 : 15 AND (Beans)1 : 11.7÷1.85		
Conclusion SALT and an accurate calculation of comparison, e.g. 3(.24) AND 7(.69), 0.3(083) AND 0.13, 30(.83%) AND 13(%), 31(%) AND 13(%), 0.31 AND 0.13 1:15 AND 1:6(.32)	B2	Ignore any units given and any additional statements if SALT unambiguously concluded with appropriate calculations evaluated correctly Accept rounded or truncated answers Ignoring units, B1 for an accurate calculation of comparison, e.g. 3(.24) AND 7(.69), 0.3(083) AND 0.13, 30(.83%) AND 13(%), 31(%) AND 13(%) 1:15 AND 1:6(.32) OR B1 for SALT with one of the two comparative values
7(c) Alternative method 1:		correct (i.e. as above with 'OR') Allow approximately or similar words for '≈'
	В3	
Conclusion SALT with evidence of a full method looking at the same number of portions, including		B2 for evidence of, e.g. 1.85 × 3(portions) ≈ 6(g) and
ratio methods, e.g.		11.7 × 8(portions) ≈ 90(g)
1.85 × 3 (portions) ≈ 6 (g)		OR (product)
AND 11.7 × 8 (portions) ≈ 90 (g)		B1 for conclusion SALT with evidence of, e.g.
		$1.85 \times 3 \text{ (portions)} \approx 6 \text{ (g)} \text{or}$
		11.7 × 8 (portions) ≈ 90 (g)
7(c) Alternative method 2: Full method with one calculated proportion, compared with same proportion of the other ingredient, e.g. • 31% salt with 0.31 × 90 • 13% sugar with 0.13 × 6	B1	
Conclusion SALT and an accurate calculation of comparison, e.g. • 27.9 (g) (sugar which is > 11.7 g in a portion) • 0.78 (g) (salt which is < 1.85 g in a portion)	B2	Ignore any units given and any additional statements if SALT unambiguously concluded with appropriate calculations evaluated correctly B1 for appropriate calculations evaluated correctly, with no or incorrect conclusion
		B1 for appropriate calculations evaluated correc

8(a) (Number of units is) 800	B1	
(Electricity cost is) 800 × 0.23 or 800 × 23	M1	FT 'their 20950 – 20150', must be from attempting this subtraction
(£)184 or 18400(p)	A1	If units are given they must be correct Accept £184.00p, do not accept £184p
(Standing charge + electricity) (£) 208 or 20800(p)	B1	FT 24 + 'their 184' provided units are consistent May be implied or embedded in further work, e.g. if 184 × 1.05 + 24 seen and calculated correctly to (£)217.2(0)
(Total bill including VAT at 5%) 1.05 × 208 or 1.05 × 20800 or equivalent	M1	FT 'their (£)208' or 'their 20800(p)', including if the standing charge is omitted (i.e. (£)184 used) Allow if standing charge is added after adding VAT to the electricity cost
(£)218.4(0) or 21840(p)	A1	CAO
(Budget per month £218.40 ÷ 3 =) (£)72.8(0) or 7280(p)	B1	FT 'their total bill' ÷ 3 provided at least 2 marks previously awarded Allow rounded up to the nearest £ On FT allow rounding to 10p, or rounding up to the nearest £
		(Note: FT answers from one month standing charge (£)201.6(0))÷ 3 = (£)67.2(0) standing charge omitted (£)193.2(0))÷ 3 = (£)64.4(0))
8(a) Alternative method:		Watch for stages in other orders, check for embedded equivalent stages
(Number of units is) 800	B1	equivalent stages
(Electricity cost is) 800 × 0.23 or 800 × 23	M1	FT 'their 20950 – 20150', must be from attempting this subtraction
(£)184 or 18400(p)	A1	If units are given they must be correct Accept £184.00p, do not accept £184p
(Budget before VAT 184÷3 + 24÷3 =) (£) 69.33(3)	B1	FT 'their 184'+ 8 provided units are consistent May be implied or embedded in further work, e.g. if (184÷3)×1.05 + 8 seen and calculated correctly to (£)72.4(0)
(Total bill including VAT at 5%) 1.05 × (184 ÷ 3 + 24 ÷ 3) or equivalent	М2	FT 'their 184 ÷ 3 + 24 ÷ 3' M1 for either of the following: • 1.05 × 'their 184 ÷ 3' (no standing charge included) • 1.05 × 'their 184 ÷ 3' + 8 (no VAT on standing charge)
(Budget per month) (£)72.8(0) or 7280(p)	A1	FT from M2 or M1 Allow rounded up to the nearest £ On FT allow rounding to 10p, or rounding up to the nearest £

8(b) 500 × 1.022 ⁵ × 1.016 ¹⁵ (500 × 1.022 ⁵ = 557.473) (500 × 1.016 ¹⁵ = 634.418 or 634.42)	M3	OR equivalent method to increase by 2.2% and to increase by 1.6% on different amounts for appropriate number of years M2 for sight of either ×1.022 ⁵ or ×1.016 ¹⁵ or equivalent calculations OR M1 for sight of either ×1.022 or ×1.016 or equivalent calculations
(£) 707.34	A1	Mark final answer, CAO, accepting answers in the range (£) 707.33 to (£) 707.35 (Note: Sight of (£)511 or (£)555 implies 500 × 1.022, from working with 2.2% of £500, M1 is awarded)
9(a)(i) (Support1 ² =) $0.9^2 + 1.1^2$	M1	Scale drawings are not accepted
Support1 ² = 2.02 or (Support1 =) $\sqrt{2.02}$	A1	Do not accept rounded to 2, unless final answer is
(Support 1 =) 1.4(2 m)	A1	1.42(1 m)** FT from M1 for the correctly evaluated square root of 'their 2.02' provided 'their answer' > 1.1 (m)
		**Note, award as follows: (Support1 ² =) $0.9^2 + 1.1^2$ M1 Support1 ² = 2 or (Support1 =) $\sqrt{2}$ A0 (Support 1 =) 1.4(1 m) A1 FT
		$(Support1^2 =) 0.9^2 + 1.1^2$ M1 $Support1^2 = 2 \text{ or } (Support1 =) \sqrt{2}$ Allow A1 if (Support1 =) 1.42(m) A1 FT
9(a)(ii) sin base angle = $\frac{1.1 + 0.8}{2.6}$	M1	OR alternative full method using Pythagoras' theorem then cos or tan
$\sin^{-1} \frac{1.1 + 0.8}{2.6}$ or $\sin^{-1} 0.73(0769)$	m1	OR FT correct statement for 'their inverse trig ratio'
(Base angle =) 46.95(°) or 47(°)	A1	Allow 46.88(°) or 46.9(°) ISW unless subtracted from 90°
		If no marks, award SC1 for an answer of 50.7(°) or 51(°) from working with Support 1
9(b) (Discount cost of bricks) (516 – 8 × 22.5(0) =) (£) 336	B1	
100 × 336 ÷ 80 or 100 × <u>336</u> 80	M1	FT 'their 516 – 8 × 22.5(0)' provided ≠ 516 and ≠ 180 for M1 and possible A1
(£) 420	A1	If no marks, award SC2 for (516 ÷ 0.8 - 180 =) (£) 465 OR SC1 for (516 ÷ 0.8 =) (£) 645 or (100 × 180 ÷ 80 =) (£) 225

10(a)(i) 120	B1	
10(a)(ii) 1800 ≤ x < 2000	B1	Accept '(£)1800 to (£)2000', or '(£)1800 – (£)2000'
10(a)(iii) Reason based on agreement due to the 4 people earning £5800 to £7800 per month or the majority of lower wages, e.g. 'the data is skewed', 'only a few of the employees will earn more than the mean wage', 'because most people employed are in the lowest 2 groups of the monthly wage' 'as the majority earn between 1800 and 2100'	E1	Allow, e.g. 'because there is a great difference between the monthly wages', 'the big numbers would affect the mean', 'more than half are in the first group' Do not accept, e.g. 'she doesn't know the exact values', 'using the median would be better', 'because there are no employees that have between 2400 and 5800 monthly wage', 'there are 64 in the first group'
10(b)(i) (2200, 48) joined to (2400, 72) joined to (3000, 80)	B2	Joined with a curve or a straight line B1 for a cumulative graph with either of the following: • correct plots but not joined, • 'their 2 plots' joined provided 1 plot 'correct' including FT plot at (3000, 48 < y ≤ 80)
10(b)(ii) £2160	B1	
10(b)(iii) 22.5(%) OR answer from correct working in the range 21(.25%) to 23.75(%) or 24(%)	B2	Working $\frac{17}{80} \times 100$ to $\frac{19}{80} \times 100$ B1 for sight of $\frac{17}{80}$ to $\frac{19}{80}$